

# Effects of Hub-to-Tip Ratio and Reynolds Number on the Performance of Impulse Turbine for Wave Energy Power Plant

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The objective of this paper is to present the performance comparison of the impulse turbines for different diameters. In the study, the investigation has been performed experimentally by model testing for some diameters, especially 0.3 m and 0.6 m. The experiment was performed for Reynolds number range of  $0.17 \times 10^5 - 1.09 \times 10^5$  and for different values of hub-to-tip ratio  $\nu$  ranging from 0.6 to 0.85. As a result, it was found that the critical Reynolds number is to be around  $0.5 \times 10^5$  for  $\nu=0.6$  and  $0.4 \times 10^5$  for  $\nu=0.7$ . For the hub-to-tip ratio, the optimum value is 0.7 when the turbine is operated at lower Reynolds number. However, its value seems to be 0.6 at higher Reynolds number in the tested range.

**Key Words :** Fluid Machinery, Impulse Turbine, Reynolds Number, Hub-to-Tip Ratio, Wave Power Conversion

## Nomenclature

$a$  : Semi-major axis of ellipse (see Fig. 1)  
 $b$  : Semi-minor axis of ellipse (see Fig. 1)  
 $C_A$  : Input coefficient,  
 $= \Delta p Q / \{ \rho (v_a^2 + U_R^2) h l_r z v_a / 2 \}$   
 $C_T$  : Torque coefficient,  
 $= T_o / \{ \rho (v_a^2 + U_R^2) h l_r z r_R / 2 \}$   
 $G$  : Distance between rotor and guide vane  
 $h$  : Rotor blade height

$l$  : Chord length  
 $l_s$  : Length of straight line (see Fig. 1)  
 $Q$  : Flow rate  
 $r_r$  : Radius of circle of rotor blade profile (see Fig. 1)  
 $r_R$  : Mean radius  
 $R_a$  : Radius of camber (see Fig. 1)  
 $Re$  : Reynolds number,  $= w l_r / (\mu / \rho)$   
 $S$  : Blade pitch  
 $t_a$  : Width of flow path (See Fig. 1)  
 $T_o$  : Output torque  
 $U_R$  : Circumferential velocity at mean radius  
 $v$  : Mean axial flow velocity  
 $w$  : Relative inflow velocity at peak efficiency point

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$z$  : Number of blades

### Greek symbols

$\Delta p$  : Total pressure drop between settling chamber and atmosphere

$\phi$  : Flow coefficient,  $= v_a / U_R$

$\eta$  : Efficiency,  $= T_o \omega / (\Delta p Q) = C_T / (C_A \phi)$

$\eta_p$  : Peak value of  $\eta$

$\mu$  : Viscosity of air

$\nu$  : Hub-to tip ratio

$\rho$  : Density of air

$\sigma$  : Solidity at mean radius

$\omega$  : Turbine angular velocity

### Subscripts

g : Guide vane

r : Rotor

## 1. Introduction

Several of the wave energy devices being studied under many wave energy program in the United Kingdom, Japan, Ireland, Portugal, India and other countries make use of the principle of an oscillating water column (OWC) (Clement et al., 2002; Falcão et al., 1993; Osawa et al., 2002; Santhakumar et al., 1998; Thorp, 2001). In such wave energy devices, a water column which oscillates due to wave motion is used to drive an oscillating air column which is converted into mechanical energy. The energy conversion from the oscillating air column can be achieved by using a self-rectifying air turbine such as a Wells turbine which was introduced by Dr. A. A. Wells in 1976. This turbine rotates in a single direction in oscillating airflow and therefore does not require a system of non-return valves. Many reports describe the performance of the Wells turbine both at running and starting conditions (Gato and Falcão, 1990; Inoue et al., 1988; Raghunathan and Tan, 1982). However, according to previous studies, the Wells turbine has inherent disadvantages: lower efficiency, poorer starting characteristics and higher noise level in comparison with conventional unidirectional turbines.

Meanwhile, in order to develop a high performance self-rectifying air turbine for wave

energy conversion, some authors have proposed the impulse turbine with self-pitch-controlled guide vanes and have clarified that the turbine can be operated with higher turbine efficiency and lower rotational speed than the Wells turbine (Setoguchi et al., 1993, 1996). This type of impulse turbine, however, has a disadvantage of maintenance of pivots on which the guide vanes are rotated automatically in a bi-directional airflow. In order to overcome this drawback, an impulse turbine with fixed guide vanes has been also proposed by the authors (Setoguchi et al., 2000). There are many reports which describe the performance of the turbine both at starting and running conditions (Setoguchi et al., 2000, 2001, 2002; Thakker et al., 2000, 2001a, 2001b, 2002). However, comparison of the performances of the impulse turbines for different diameters have not been shown so far. It is important for practical use to clarify the scale effect of the impulse turbine with fixed guide vanes.

The objective of this paper is to present the performance comparison of the impulse turbines for different diameters. In the study, the investigation has been performed experimentally by model testing for some diameters, especially 0.3 m and 0.6 m. The experiment was performed for Reynolds number range  $Re$  of  $0.17 \times 10^5 - 1.09 \times 10^5$  and for different values of hub-to-tip ratio  $\nu$  ranging from 0.6 to 0.85.

## 2. Experimental Apparatus and Procedure

The experiments have been carried out by using the test facilities of Saga University (Japan) and Wave Energy Research Team at University of Limerick (Ireland) (these are named as SU and WERT respectively in the following discussions). A schematic view of the test rig of SU is shown in Setoguchi et al (2001, 2002). This test rig consists of a large piston-cylinder (diameter: 1.4 m, length: 1.7 m), a settling chamber and a 300-mm-diameter test section with the inlet and outlet bell-mouth. The turbine rotor is placed at the center of the test section and tested under any flow conditions. In testing the turbine characteristics,

the variations of turbine performance with flow coefficient  $\phi$  were examined by changing the rotational speed of the rotor step by step from a low speed to high speed, so as to cover the effective operating range of the turbine. The uncertainty with 95% confidence interval is  $\pm 1\%$  for the measured turbine efficiency  $\eta$ .

The detail information of the test apparatus of WERT is shown in Thakker et al (2002). It consists of a bell mouth entry, 0.6 m test section, drive and transmission section, a plenum chamber with honeycomb section, a calibrated nozzle and a centrifugal fan. The turbine was mounted on a shaft in a cylindrical annular duct. The shaft coupled to a motor/generator via a downstream hub of the rig. The uncertainty with 95% confidence interval in the results, based on instrument's accuracy was within  $\pm 1.5\%$ .

In both the above facilities, the overall performance was evaluated in term of the turbine angular velocity  $\omega$ , the output torque  $T_o$ , the flow rate  $Q$  and the total pressure drop  $\Delta p$  between the settling chamber and the atmosphere. Tests were performed under steady flow conditions.

As shown in Fig. 1, the turbine configuration employed is the impulse turbine having fixed guide vanes both upstream and downstream, and these geometries are symmetrical with respect to the rotor centerline. The rotor blade profile consists of a circular arc on the pressure side and part of an ellipse on the suction side. For the size of the ellipse, the ratio of the semi-major axis to semi-minor axis  $a/b$  is 3.0. The ratio of the

radius of the circle on the pressure side to the chord length  $r_r/l_r$  is 0.56. The blade inlet (or outlet) angle and the thickness ratio are  $60^\circ$  and 0.3, respectively. The specification of rotor blades used is shown in Table 1. The guide vanes are symmetrically installed at the distance of  $G$  downstream and upstream of the rotor. The camber line of guide vane consists of a straight line and a circular arc. The specification of the guide vane adopted in the experiments is shown

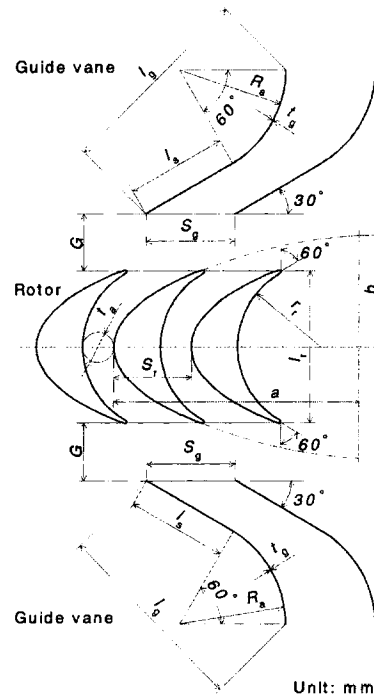


Fig. 1 Turbine configuration

Table 1 Specification of rotor blades

Research institution	Hub-to-tip ratio $\nu$	Tip diameter [mm] (Tip clearance[mm])	Solidity $\sigma_r (=l_r/S_r)$ (No. of blades $z_r$ )	Reynolds number at peak efficiency point $Re[\times 10^5]$	Chord length $l_r$ [mm]
Saga University (SU)	0.6	298(1.0)	2.01(28)	0.17–0.45	54
	0.65		2.01(29)	0.38	
	0.7		2.02(30)	0.22–0.51	
	0.75	278.6(0.7)	2.03(29)	0.44	
	0.85	246(0.5)	2.03(27)	0.60	
University of Limerick (WERT)	0.6	598(1.0)	2.00(30)	0.38–1.00	100
	0.7		1.99(30)	0.40–1.09	106

**Table 2** Specification of guide vanes

Research institution	Hub-to-tip ratio $\nu$	Solidity $\sigma_g (=l_g/S_g)$ (No. of vanes $z_g$ )	Chord length $l_g$ [mm]	Radius of camber $Ra$ [mm]	Length of straight line $l_s$ [mm]
Saga University (SU)	0.6	2.23(24)	70	37.2	34.8
	0.65	2.25(25)			
	0.7	2.27(26)			
	0.75	2.27(25)			
	0.85	2.24(23)			
University of Limerick (WERT)	0.6	2.27(26)	131.4	69.6	65.3
	0.7	2.27(26)	139.5	73.9	69.2

in Table 2. It may be noted that the rotor solidity  $\sigma_r$  and the guide vane solidity  $\sigma_g$  at the mean radius  $r_R$  for the tested turbines are almost the same as the most promising one in the previous studies (Setoguchi et al., 2000, 2001).

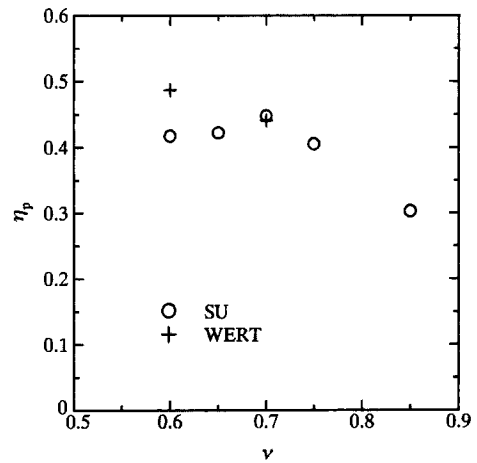
The values of hub-to-tip ratio  $\nu$  adopted in the study are 0.6, 0.65, 0.7, 0.75 and 0.85 for SU, and 0.6 and 0.7 for WERT. In the SU test rig, the effect of  $Re$  was tested for ranges of  $0.17 \times 10^5 - 0.45 \times 10^5$  for  $\nu=0.6$  and  $0.22 \times 10^5 - 0.51 \times 10^5$  for  $\nu=0.7$ , respectively. For the facility of WERT, the ranges of  $Re$  are  $0.38 \times 10^5 - 1.00 \times 10^5$  for  $\nu=0.6$  and  $0.40 \times 10^5 - 1.09 \times 10^5$  for  $\nu=0.7$ . The above experiments have been performed by changing the flow rate  $Q$  and the angular velocity  $\omega$ . The detail information is shown in Table 1.

### 3. Experimental Results and Discussions

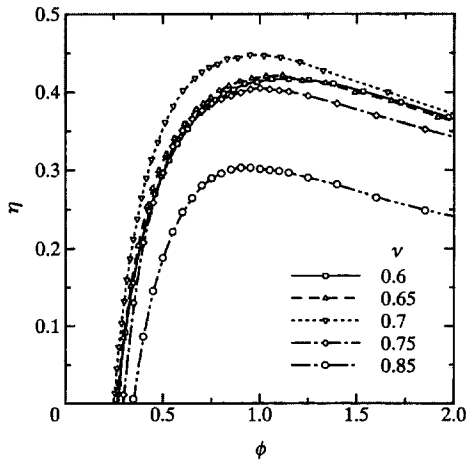
#### 3.1 Effect of hub-to-tip ratio

The turbine performance under steady flow conditions is evaluated by turbine efficiency  $\eta$ , torque coefficient  $C_T$  and input coefficient  $C_A$  against flow coefficient  $\phi$ .

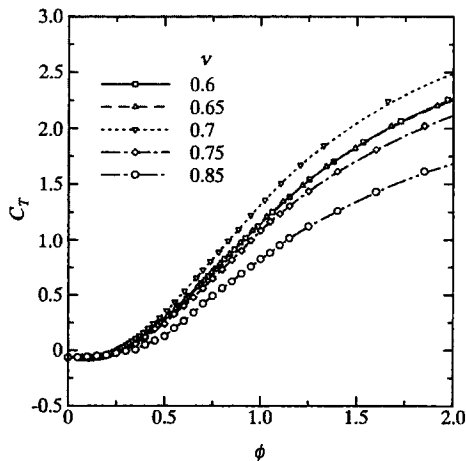
Figures 2 and 3 shows the effect of hub-to-tip ratio  $\nu$  on turbine characteristics under steady flow conditions, which are obtained by the facility of SU. It can be observed that the turbine peak efficiency  $\eta_p$  increases with  $\nu$  for  $\nu \leq 0.7$  (Fig. 2), though the trend of all the tested hub-to-tip ratio is qualitatively the same { Fig. 3(a)}. Now, let us discuss the reason using both the

**Fig. 2** Effect of hub-to-tip ratio on peak efficiency

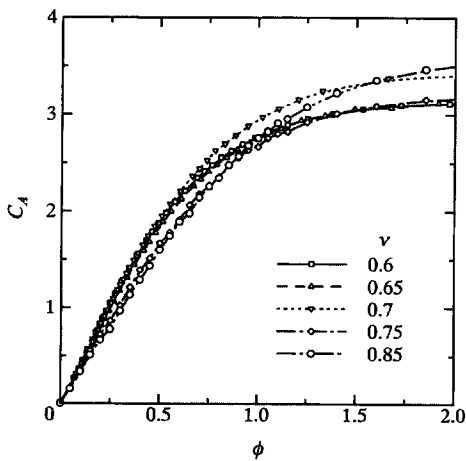
$C_T - \phi$ ,  $C_A - \phi$  characteristics { Figs. 3(b) and 3(c)} and the velocity diagram. Comparing the values of  $C_T$  and  $C_A$  for  $\nu=0.6$  with that for  $\nu=0.7$ , a rate of decrease in  $C_T$  is larger than that in  $C_A$ . We consider that this phenomenon is because a difference between the incidence angle at tip and at near the hub increases with decreasing  $\nu$  for a turbine operating at a certain speed. That is, it should be expected that the incidence angle at tip becomes large when the  $\nu$  is small, and then the boundary layer separation occurs on the pressure side at the leading edge and on the suction side at maximum thickness point of the rotor blade (Kinoue et al., 1999). Consequently, the decrease of hub-to-tip ratio leads to the deterioration of  $T_o$  and  $\eta$ . Meanwhile, the  $\eta_p$  decreases with increasing  $\nu$  for  $\nu \geq 0.7$  because the  $C_T$  decreases with the decrease of  $\nu$  in a whole



(a) Efficiency

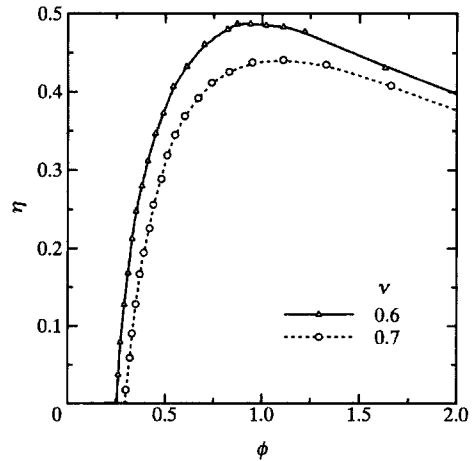


(b) Torque coefficient

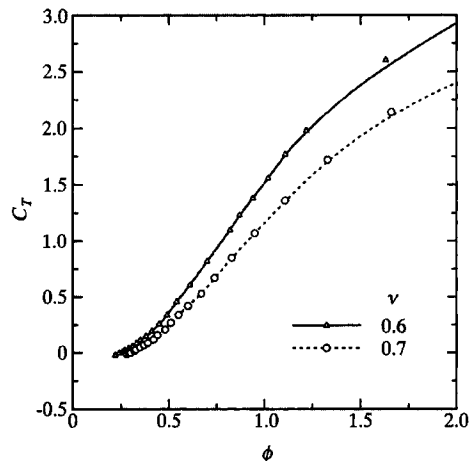


(c) Input coefficient

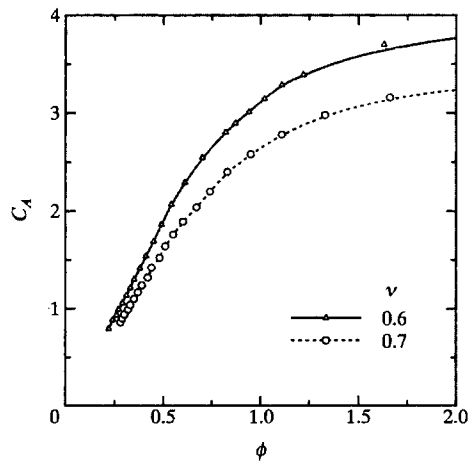
**Fig. 3** Effect of hub-to-tip ratio on turbine characteristics (SU)



(a) Efficiency



(b) Torque coefficient



(c) Input coefficient

**Fig. 4** Effect of hub-to-tip ratio on turbine characteristics (WERT)

of  $\phi$  as shown in Fig. 3(b).

Conversely, in the case of WERT, the  $\eta_p$  for  $\nu=0.6$  is higher than that for 0.7 as shown in Figs. 2 and 4(a). This result is the opposite of SU's one. Particularly, it should be noted that the difference of  $\eta_p$  between WERT and SU is as much as seven percent at  $\nu=0.6$  (Fig. 2). The reason can be considered from the comparison of  $C_T$  for both the test facilities as shown in Fig. 5. In the case of  $\nu=0.7$ , the  $C_T$  for SU is slightly higher than that for WERT { Fig. 5(b)}. However, for  $\nu=0.6$ , the value for WERT is better than that for SU { Fig. 5(a)}. This is because boundary layer separation at tip is restrained by

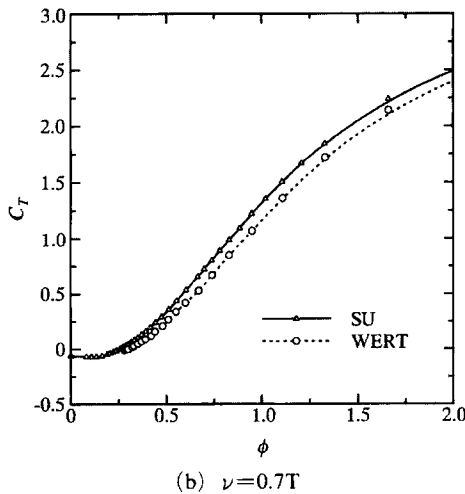
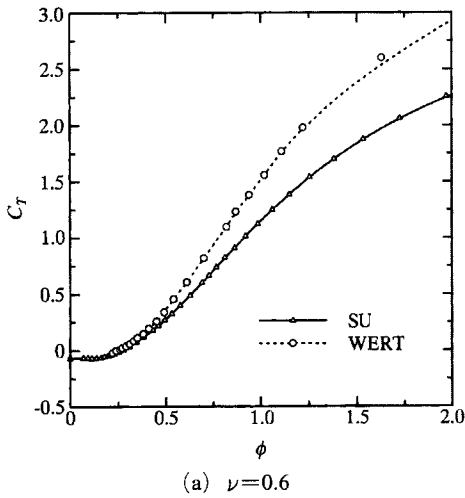


Fig. 5 Comparison of torque coefficient for impulse turbines with different diameters

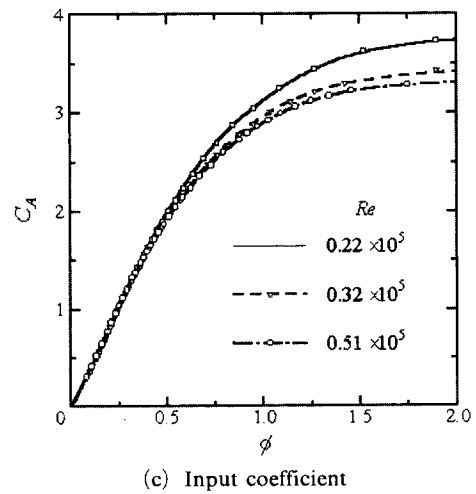
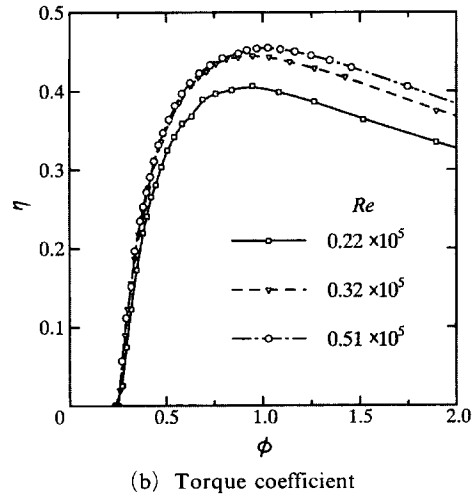
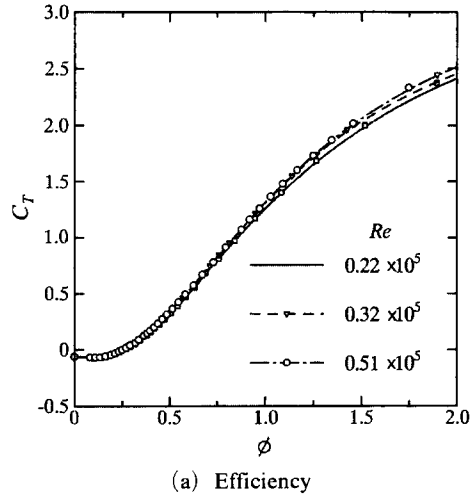


Fig. 6 Effect of Reynolds number on turbine characteristics (SU,  $\nu=0.7$ )

the influence of Reynolds number effect.

Therefore, it is concluded from the results obtained in this study that the optimum value of  $\nu$  of the impulse turbine with fixed guide vanes for wave power conversion is approximately 0.7 when the turbine is operated at lower Reynolds number. However, its value seems to be 0.6 at higher Reynolds number in the tested range.

### 3.2 Effect of Reynolds number

For practical use, it is necessary to investigate the effect of Reynolds number  $Re$  on turbine performance. In the study, the experiments have been carried out for four turbines with various hub-to-tip ratios and diameters.

Figure 6 shows the turbine characteristics under steady flow conditions for three Reynolds number, for 0.3 m impulse turbine with  $\nu=0.7$ . The efficiency increases with  $Re$  in the entire range of  $\phi$  (Fig. 6(a)). This is because the  $C_T$  slightly increases with  $Re$ , and the  $C_A$  decreases with  $Re$  due to the viscous influence at lower  $Re$  (Figs. 6(b) and 6(c)). Therefore, as is evident from the definition of  $\eta$ , the  $\eta$  increases with  $Re$ .

Figure 7 shows the effect of Reynolds number  $Re$  on peak efficiency  $\eta_p$  for  $\nu=0.6$  and 0.7. The experiments have been carried for 0.3 m and 0.6 m turbines. The value of  $\eta_p$  for  $\nu=0.7$  increases gradually in the case of both the turbines and

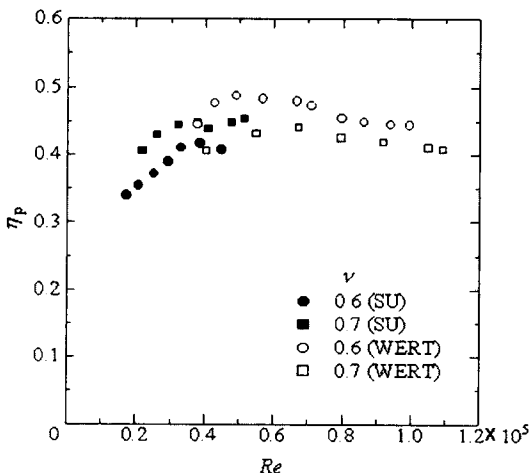


Fig. 7 Effect of Reynolds number on peak efficiency

then remains almost constant for  $Re \geq 0.4 \times 10^5$ . However, in the case of  $\nu=0.6$ , the value of  $\eta_p$  remains almost constant for  $Re \geq 0.5 \times 10^5$ . Therefore, it is believed from the fact that the critical Reynolds number of the impulse turbine seems to be approximately  $0.5 \times 10^5$  for  $\nu=0.6$  and  $0.4 \times 10^5$  for  $\nu=0.7$ .

## 4. Conclusions

The effects of Reynolds number  $Re$  and hub-to-tip ratio  $\nu$  on the performance of the impulse turbine for wave energy conversion have been investigated experimentally by model testing under steady flow conditions. As a result, it was found that the critical Reynolds number is to be around  $0.5 \times 10^5$  for  $\nu=0.6$  and  $0.4 \times 10^5$  for  $\nu=0.7$ . For the hub-to-tip ratio, the optimum value is 0.7 when the turbine is operated at lower Reynolds number. However, its value seems to be 0.6 at higher Reynolds number. A future study may seek to clarify the effect of hub-to-tip ratio at higher Reynolds number for  $\nu < 0.6$ .

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